One more step towards well-composedness of cell complexes over nD pictures

Nicolas Boutry $^{\ast 1},$ Rocio Gonzalez-Diaz $^{\ast 2},$ and Maria-Jose Jimenez $^{\ast 2}$

¹Laboratoire de Recherche et de Développement de lÉPITA (LRDE) – Ecole Pour l'Informatique et les Techniques Avancées – LRDE, EPITA 14-16, rue Voltaire F-94276 Le Kremlin Bicêtre cedex France,

France

²Universidad de Sevilla – Spain

Abstract

An nD pure regular cell complex K is weakly well-composed (wWC) if, for each vertex v of K, the set of n-cells incident to v is

face-connected. In previous work we proved that if an nD picture I is digitally well composed (DWC) then the cubical complex Q(I) associated to I is wWC. If I is not DWC, we proposed a combinatorial algorithm to "locally repair" Q(I) obtaining an nD pure simplicial complex P_S (I) homotopy equivalent to Q(I) which is always wWC. In this paper we give a combinatorial procedure to compute a simplicial complex $P_S(\overline{\{I\}})$ decomposes the complement space of $|P_S(I)|$ and prove that $P_S(\overline{\{I\}})$ is alsow WC. This paper means one more step or toprove that then Drepaired complex is continuously well - composed (CWC), that is, the boundary of its continuous analogist -1) - manifold.